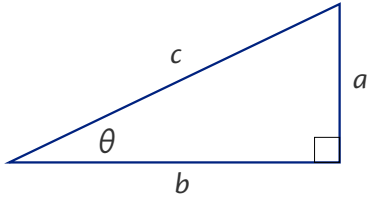


## Trigonometric Functions ("SohCahToa")



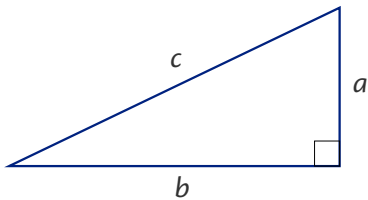
$$\sin \theta = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{a}{c}$$

$$\cos \theta = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{b}{c}$$

$$\tan \theta = \frac{\text{opposite}}{\text{adjacent}} = \frac{a}{b}$$

## Triangles

### Pythagorean Theorem and Friends



Right triangle:  $c^2 = a^2 + b^2$

Obtuse triangle:  $c^2 > a^2 + b^2$

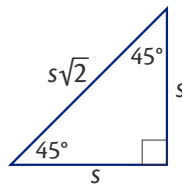
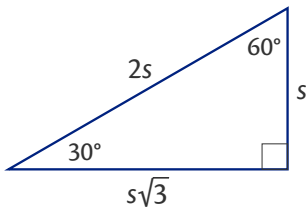
Acute triangle:  $c^2 < a^2 + b^2$

Seriously, memorize these; they'll keep showing up the rest of your math career.

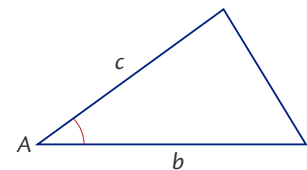
#### Pythagorean Triplets

- 3-4-5
- 5-12-13
- 7-24-25

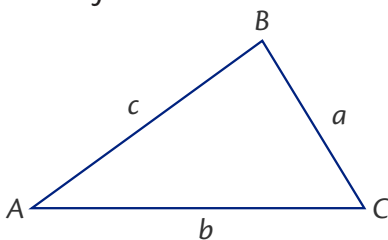
### Special Triangles



#### Area of an Arbitrary Triangle

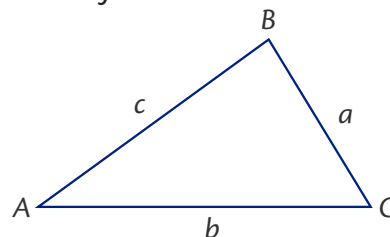


### Law of Sines



$$\frac{\sin A}{a} = \frac{\sin B}{b} = \frac{\sin C}{c}$$

### Law of Cosines



$$a^2 = b^2 + c^2 - 2bc \cos(A)$$

## Law of Sines, Ambiguous Case

---

### Number of possible triangles

Given a triangle in which you know angle-side-side, as at right.

- Calculate  $h = b \sin \theta$

Note that  $b$  is the side adjacent to the angle

- Compare  $h$  and  $a$  (the far side)

$h > a$             No triangle

$h = a$             One triangle (no ambiguity)

$h < a$             Possibly two triangles

